

STATISTICAL MECHANICS FOR COMPLEXITY

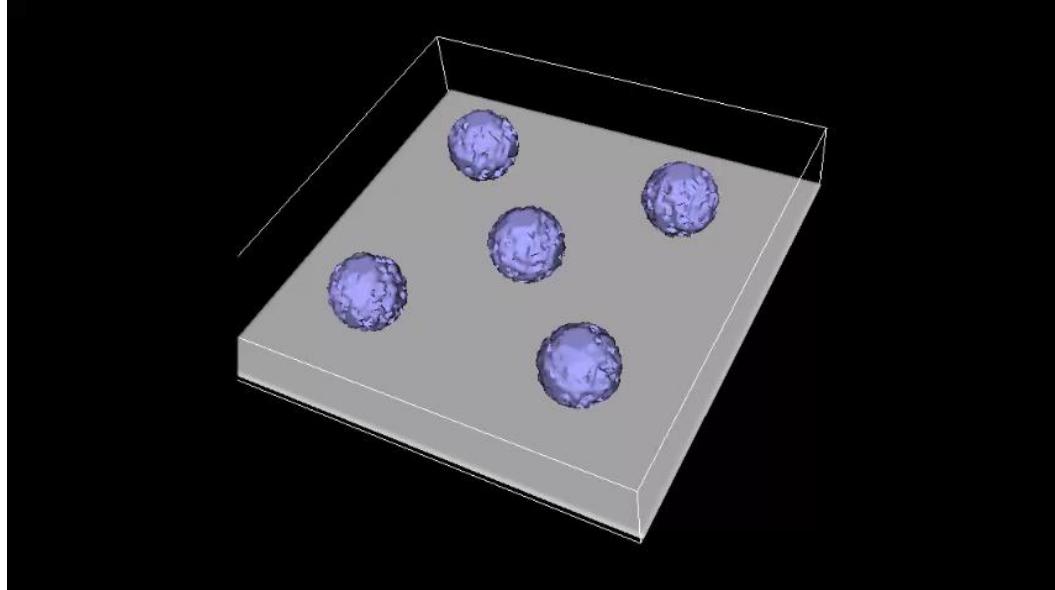
A CELEBRATION OF THE 80TH BIRTHDAY OF CONSTANTINO TSALLIS

RIO DE JANEIRO, 6 TO 10 NOVEMBER 2023



A Project!

Epithelial-Mesenchymal transformation, cell migration, and active solids.



Rita M.C.de Almeida

IF-UFRGS

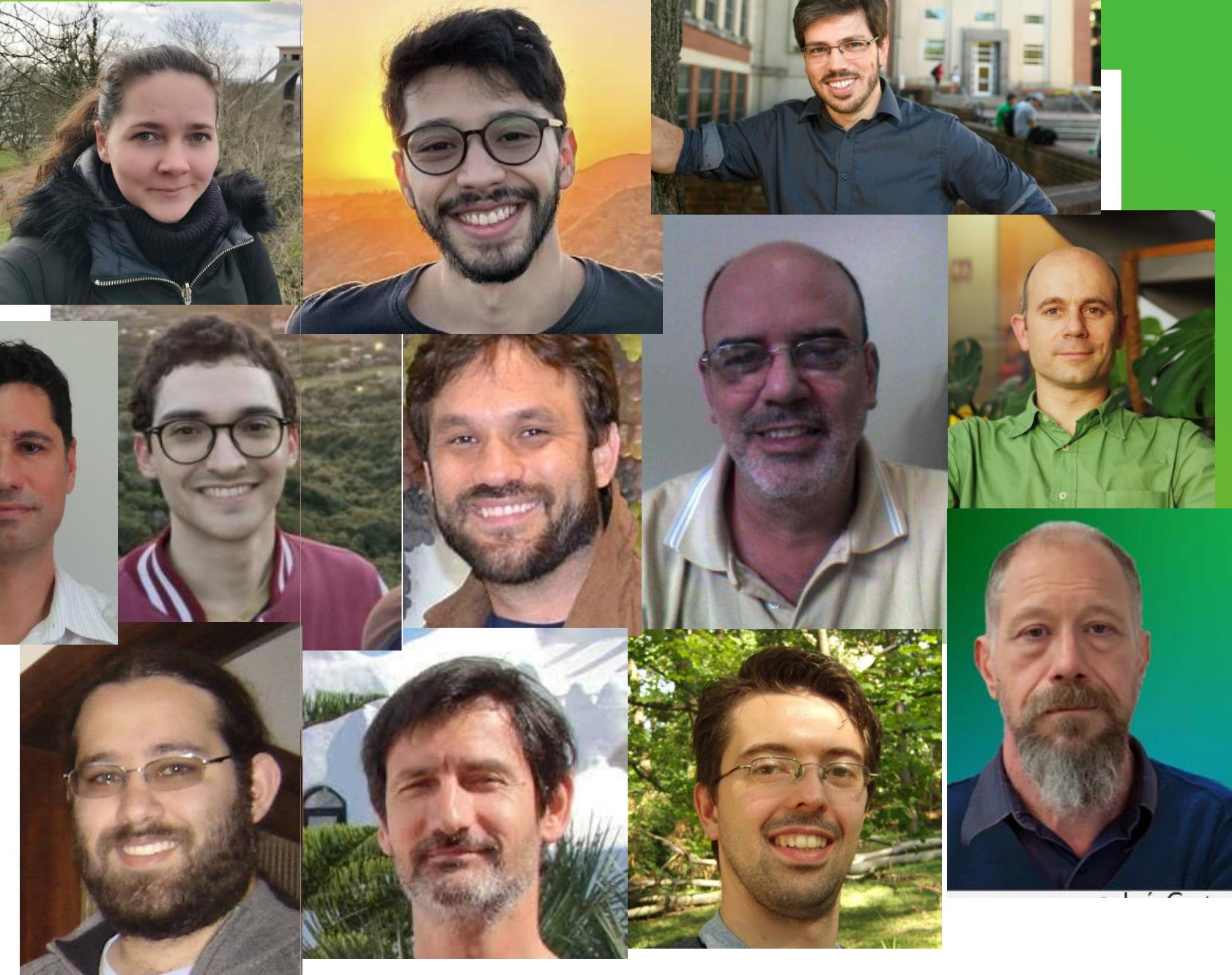
PPG em Bioinformática - UFRN

INCT: Sistemas Complexos



Collaborators

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- + Gabriel C. Perrone
- + Mendeli Vainstein
- + Carine Beatrici



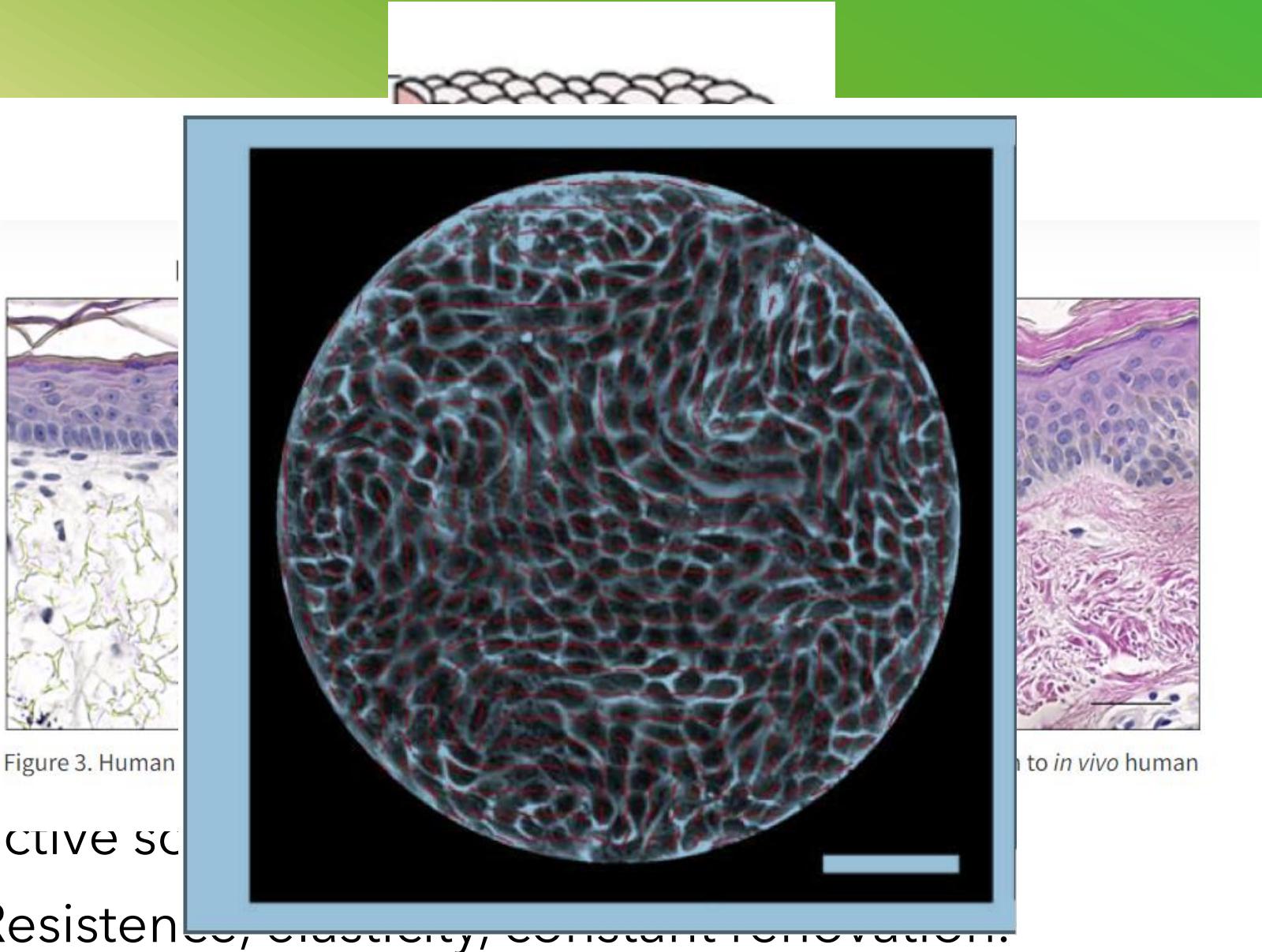
Epithelial –mesenchymal transformation (EMT)

- + From epithelial to mesenchymal phenotype
- + MET (mesenchymal to epithelial)
- + Wound healing
- + Development
- + Metastases.

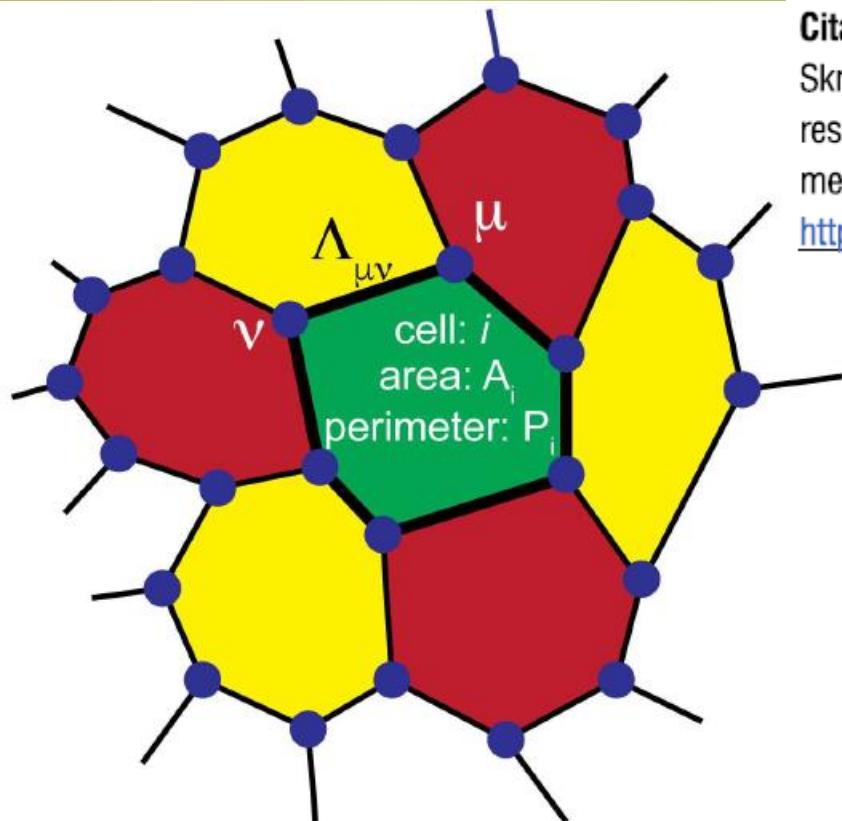
[wound healing assay - Pesquisa Google](#)

C

- + Figure 3. Human
- + active sc
- + Resistance, elasticity, constant regeneration...



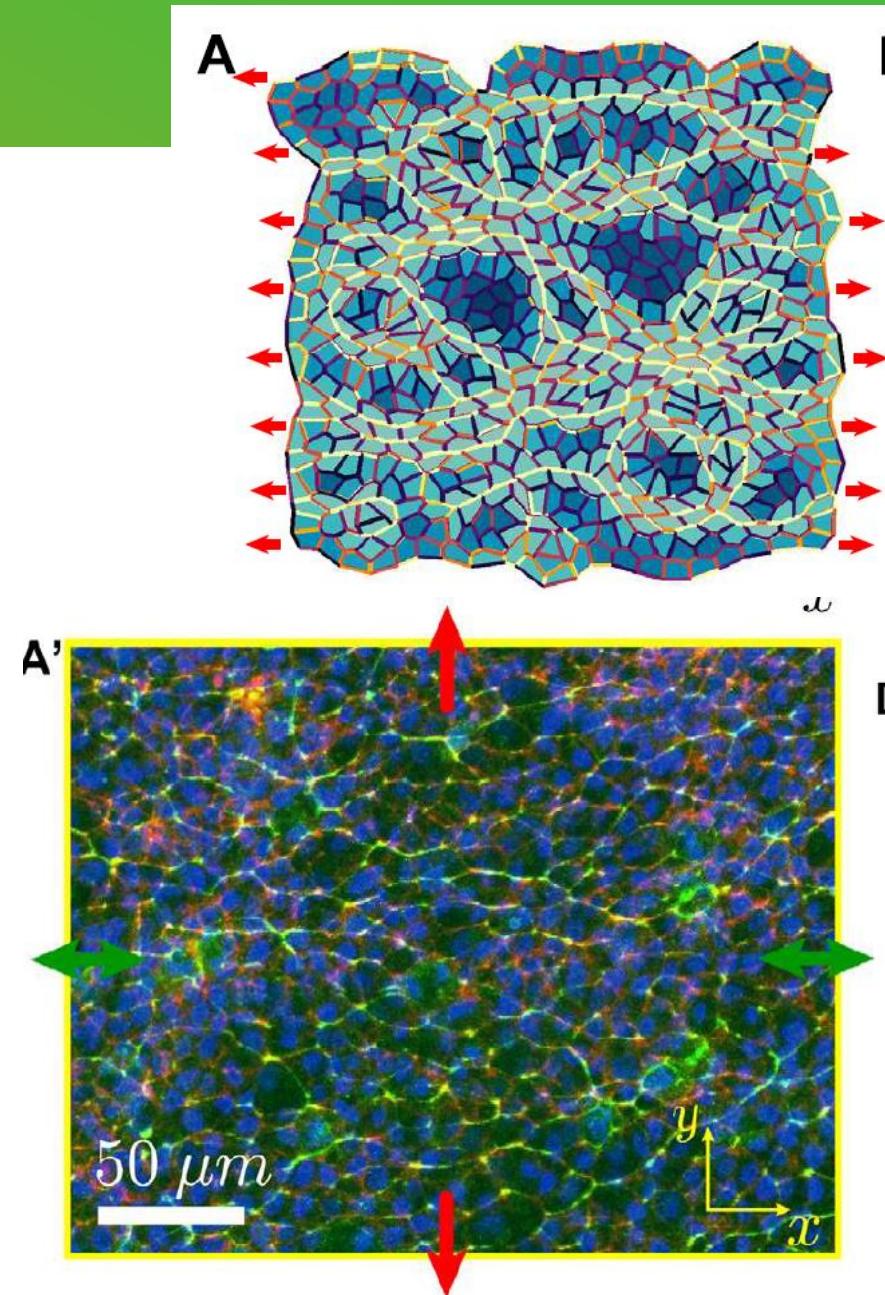
Vertex model



Citation: Barton DL, Henkes S, Weijer CJ, Sknepnek R (2017) Active Vertex Model for cell-resolution description of epithelial tissue mechanics. PLoS Comput Biol 13(6): e1005569. <https://doi.org/10.1371/journal.pcbi.1005569>

Fig 1. In the Vertex Model (VM), a confluent epithelial sheet is represented as a polygonal tiling of the plane with no holes or overlaps. Each cell is represented by an n -sided polygon. Neighbouring cells share an edge, which models the cell junction as a straight line. Three edges meet at a vertex (dark blue dots). The behaviour of cell i is described by three parameters: 1) reference area A_i^0 , 2) area modulus K_i , and 3)

$$E_{VM} = \sum_{i=1}^N \frac{K_i}{2} (A_i - A_i^0)^2 + \sum_{i=1}^N \frac{\Gamma_i}{2} P_i^2 + 2 \sum_{\langle \mu, \nu \rangle} \Lambda_{\mu\nu} l_{\mu\nu},$$



Mesenchymal cells

- + Migration
- + Chemotaxis
- + Adhesion to matrix componentes (fibers)
- + Rear-front polarization.

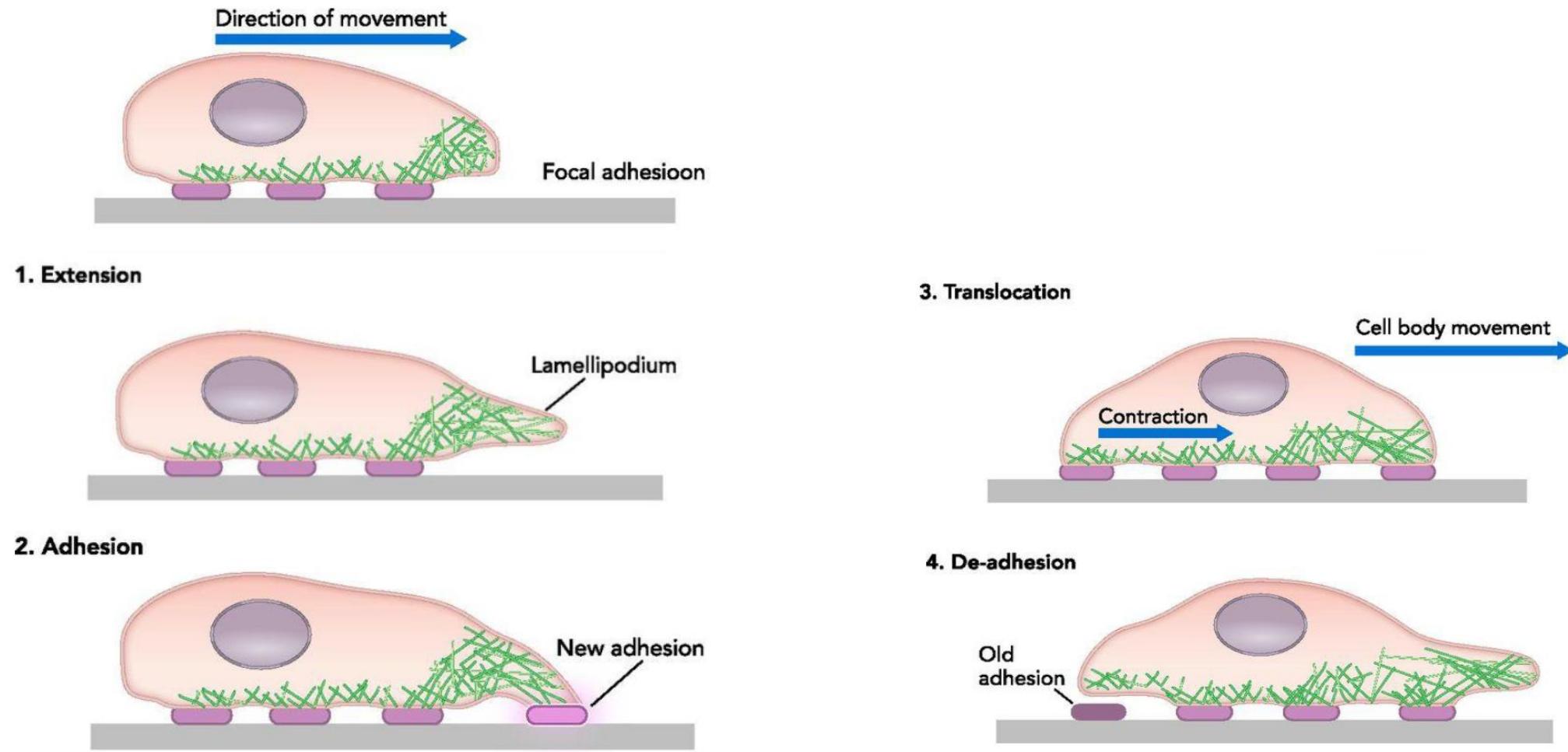
https://www.google.com.br/search?q=wound+healing+assay&source=lmns&tbs=vid&hl=pt-BR&sa=X&ved=2ahUKEwjL-cWfgv6BAxWePrkGHdqSDJgQ_AUoAnoECAEQAg#fpstate=ive&vld=cid:e9b3e2b0,vid:OWC8pGMqza0,st:0

BMDC WT
2D + Confinement
30°C

BMDC 2D + Confinement

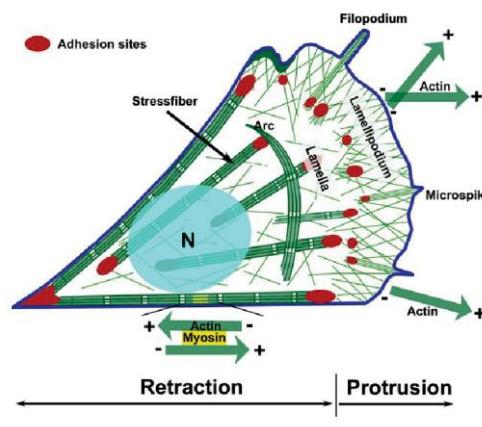
Diffusive

Abercrombie model



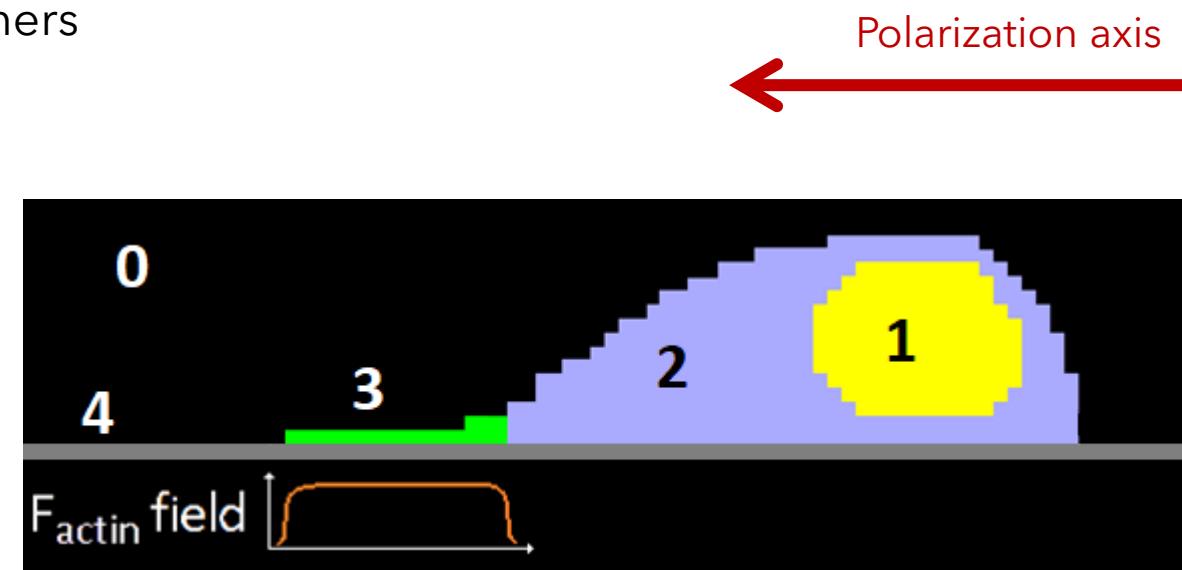
Design:

- 0 - Medium
- The Cell: 3 compartments
 - 1. Nucleus
 - 2. Cytoplasm
 - 3. Lamellipodium (Front)
- 4 - Substratum
- Actin cortex
 - density fields (actin polymers represented by F-Actin)
- No focal contacts

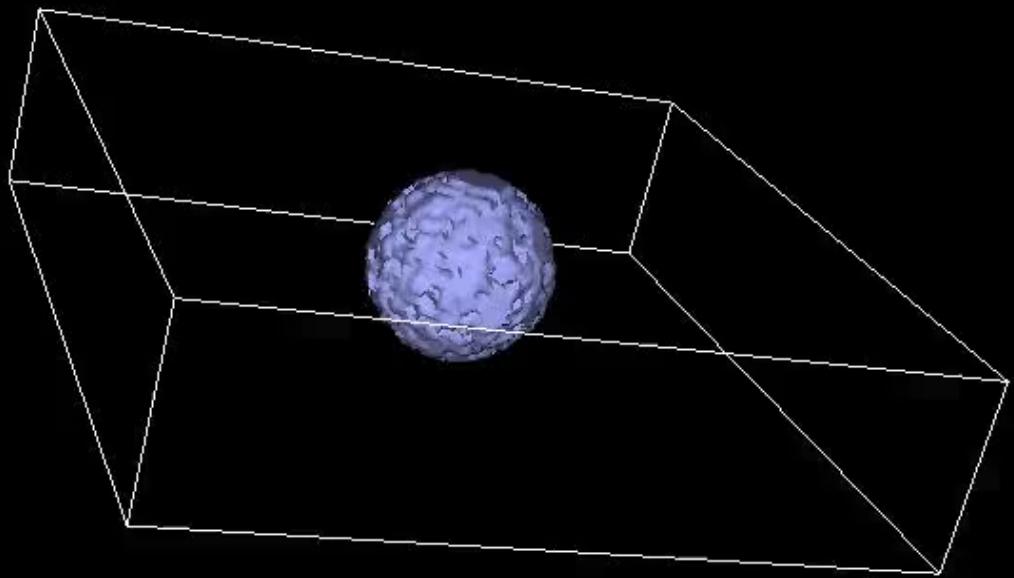
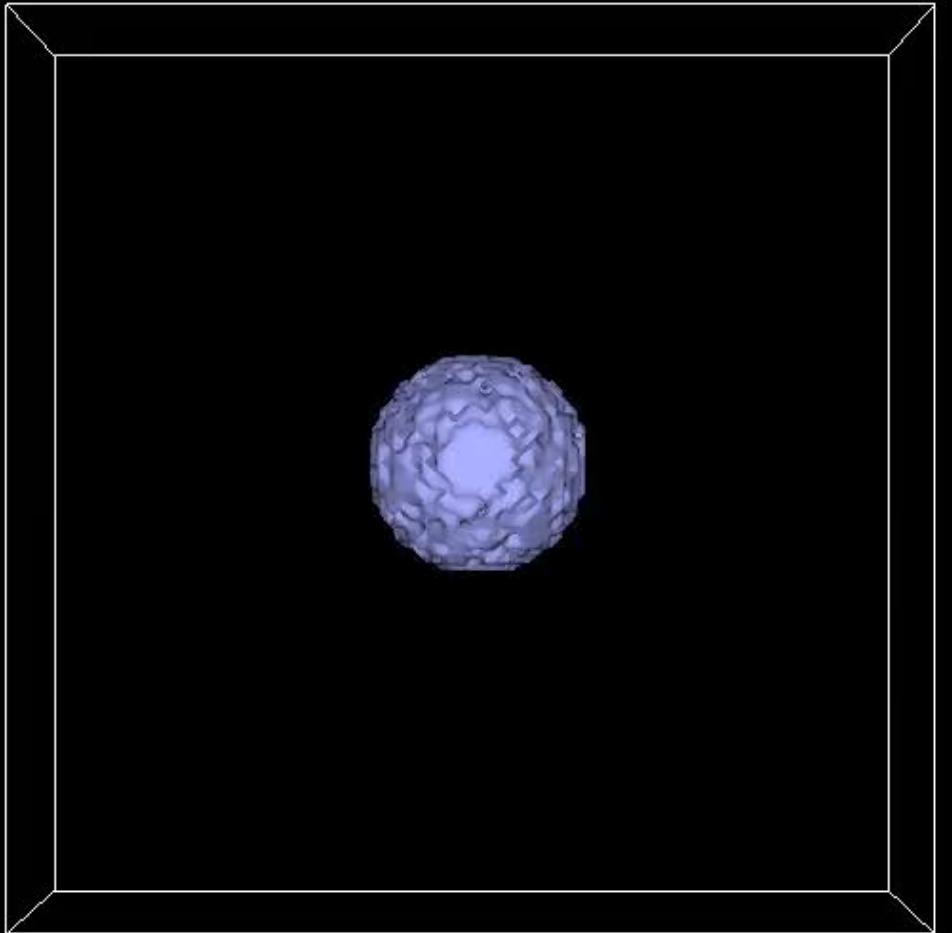


Dynamics:

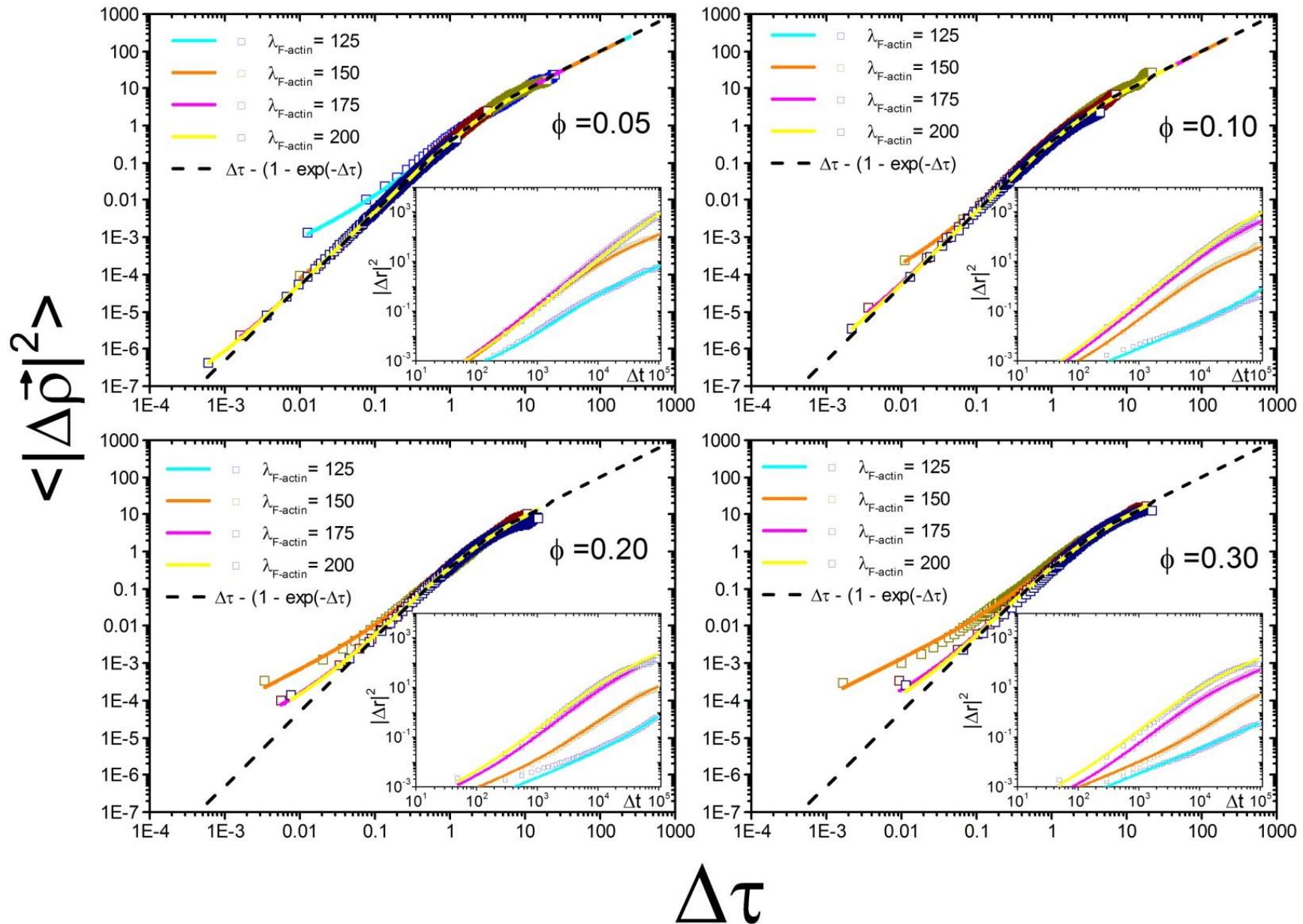
- 1) F-actin favors the overwriting of medium lattice sites (**black**) by lamellipodium (**green**) lattice sites
- 2) The volume constraint of the cell compartments backpropagates the lamellipodium extension and causes the cell to displace
- 3) The cell acquires a **polarization axis**, which causes the cell to migrate persistently in the direction of polarization



Schematic representation of the simulated cell by Ismael Fortuna



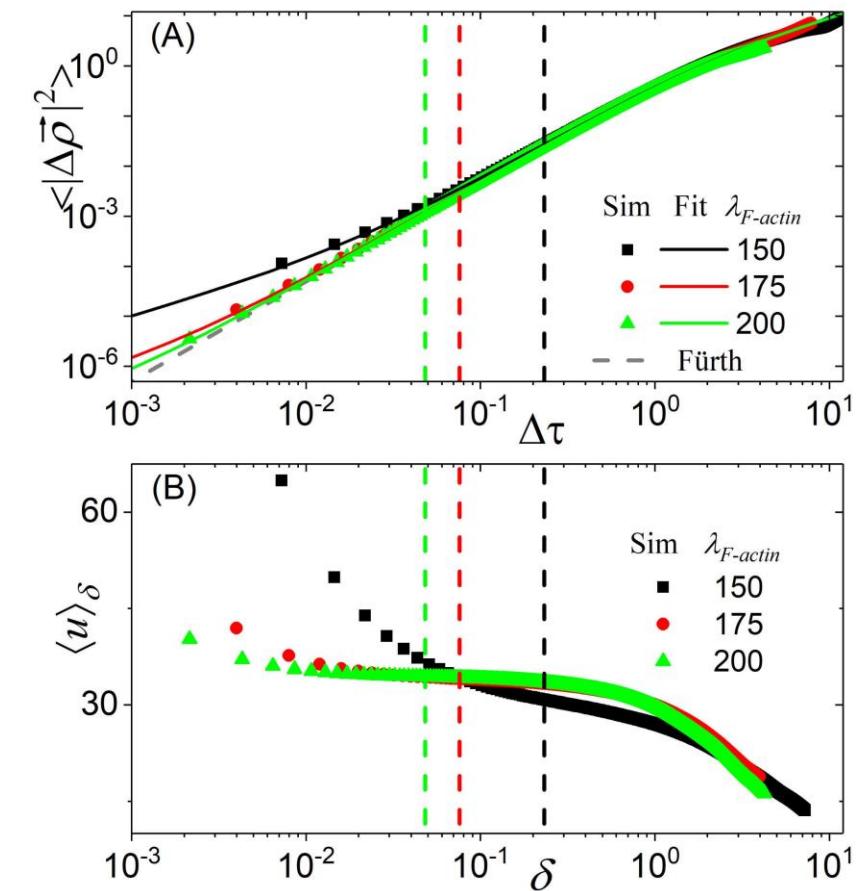
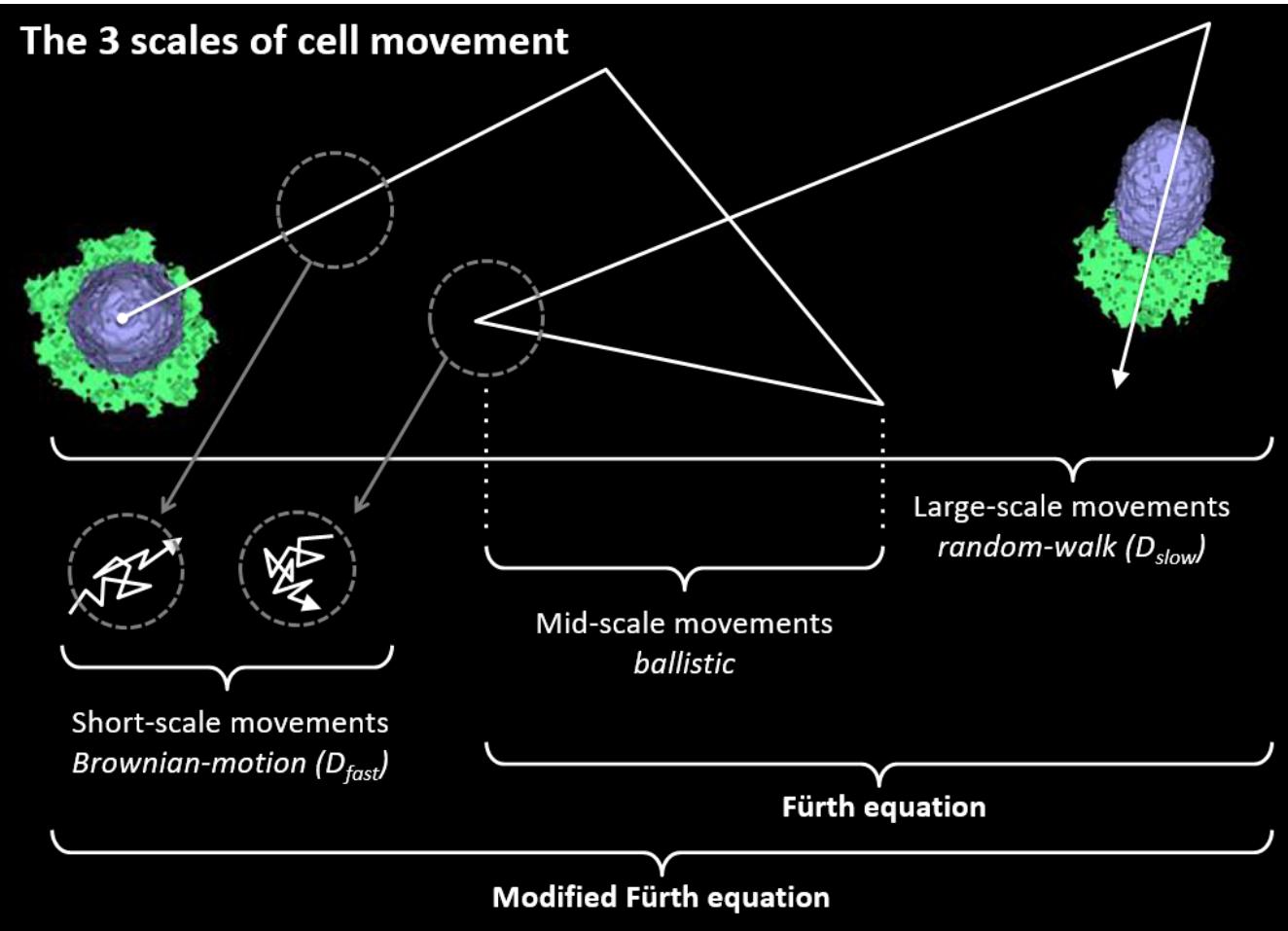
Modified Furth Equation

 $R=15$ 

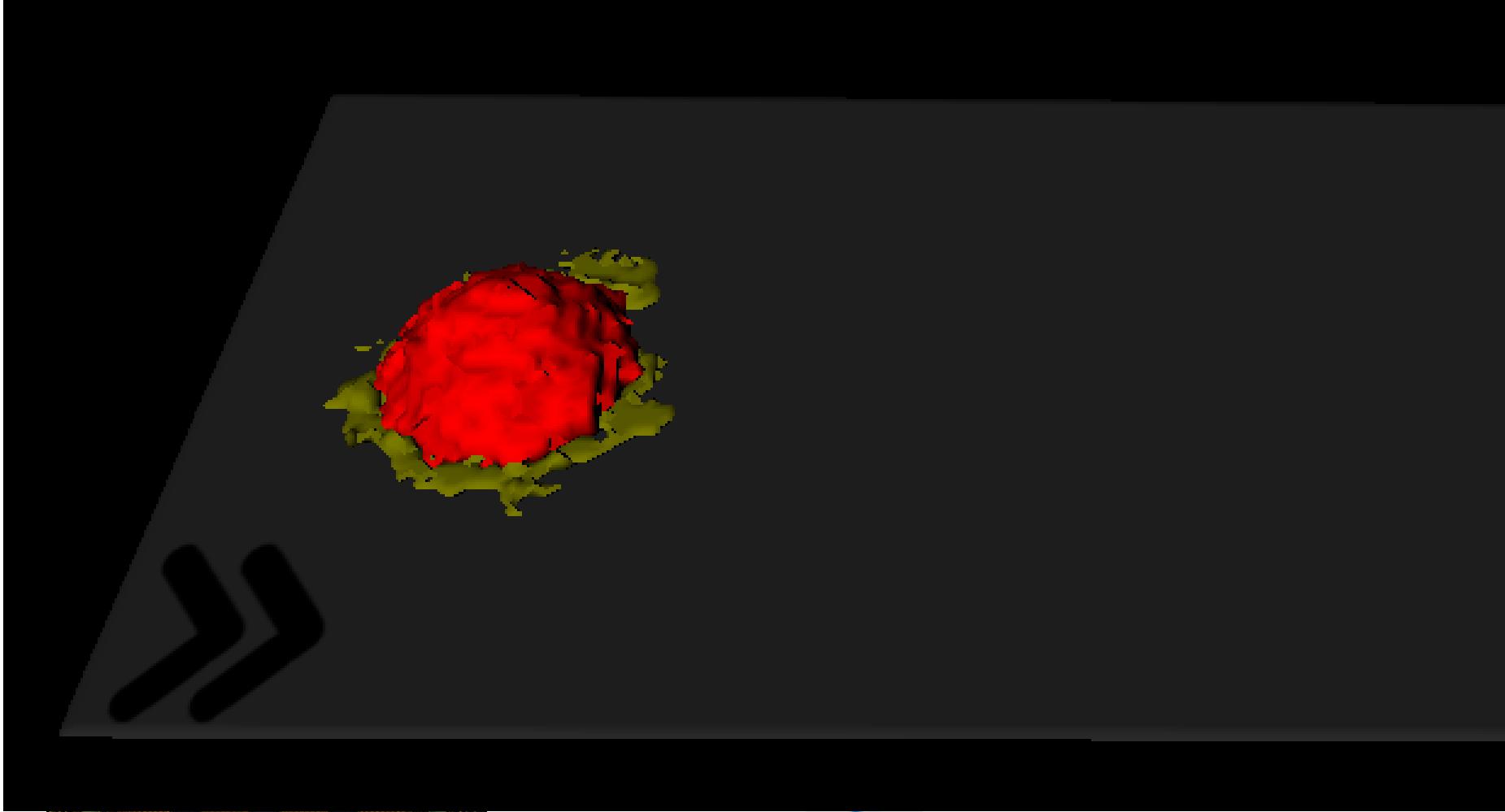
Cell geometry and movement are correlated.

Are They?

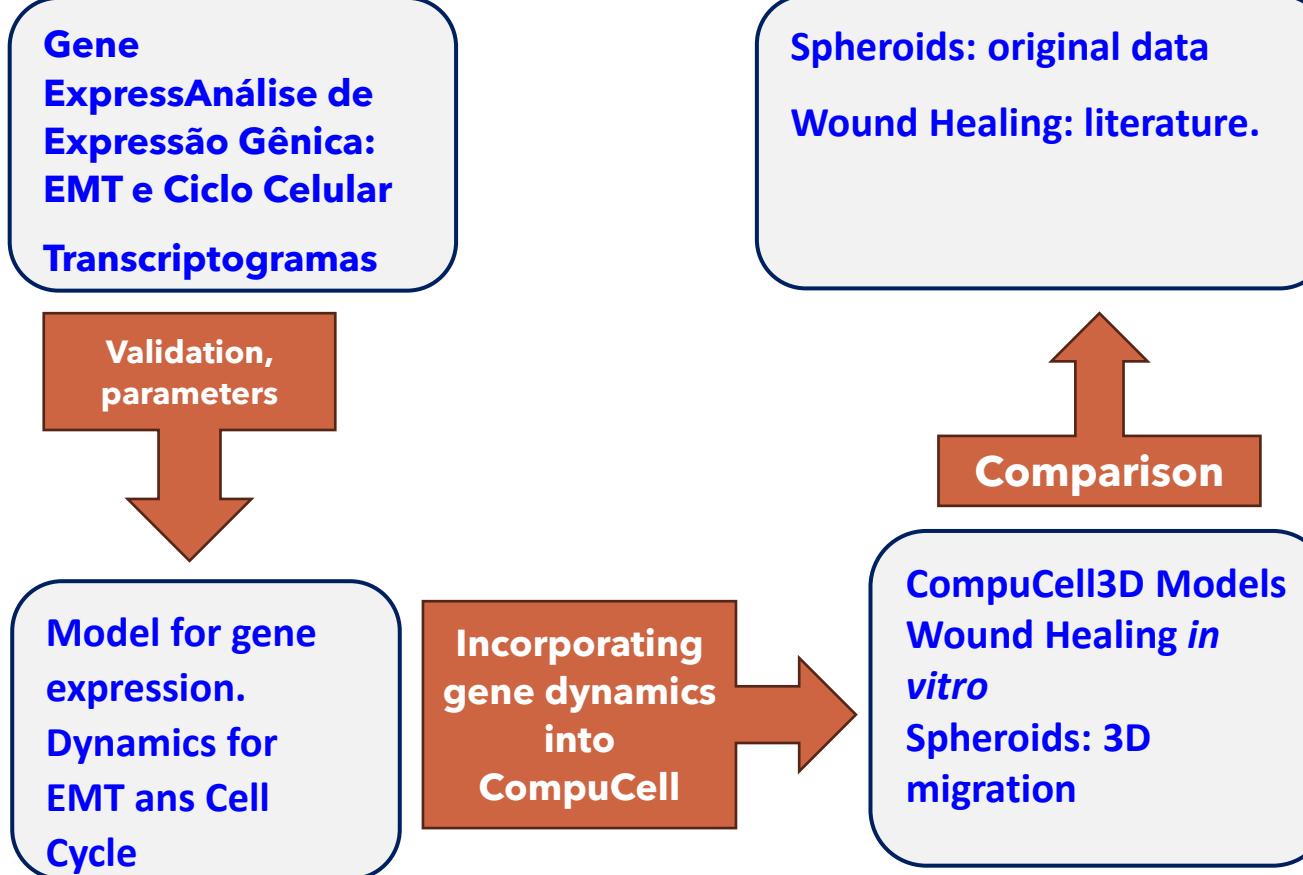
How simulations may help.



Chemotaxis



BACK to EMT



Regulatory gene networks and EMT

- + Cell life is a manifestation of biochemical reaction involving many thousands of proteins, RNAs and metabolites.
- + Non-linear reactions, interactions with cell environment.
- + Feed back loops
- + Many attractors. Stable phenotypes associated with attractors.
- + External stimuli may trigger the transition between attractors
- + EMT is such a case.(?)

Tripathi, Kessler, Levine
PRL,125, 088101 (2020); PNAS 120, e2216109120 (2023)

Biological networks are minimally frustrated

- + Simple models work;
- + Different models work.
- + There are Boolean models.

Inspired by spin systems!

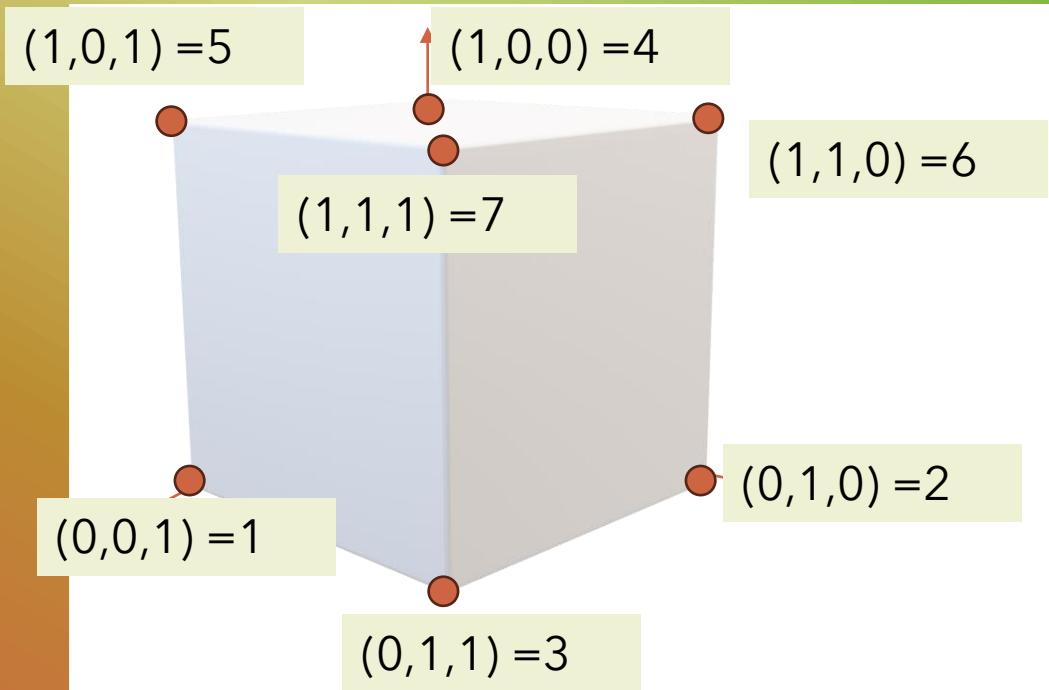
$$s_i(t+1) = \begin{cases} +1 & \sum_j J_{ij} s_j > 0 \\ -1 & \text{if } \sum_j J_{ij} s_j < 0 \\ s_i(t) & \sum_j J_{ij} s_j = 0. \end{cases} \quad (1)$$

Stable states in biological networks have large basins of attraction and the stable states are minimally frustrated.

Random networks: J_{ij} may assume -1,0,1 and are randomly chosen.

Comparison with biological systems with the same connections.

Information Space dynamics



$$\sigma=0, 1, 2, \dots, 2^M - 1$$

$y(\sigma, t)$: Intensidade de expressão da info σ

De Almeida, Espinosa, Idiart
PRE 74, 041912 2006

$$a(t) = \sum_{\sigma=0}^{2^M-1} y(\sigma, t),$$

$$\langle \tilde{S}_i(t) \rangle a(t) = \sum_{\sigma=0}^{2^M-1} y(\sigma, t) \sigma_i,$$

$$\langle \tilde{S}_i(t) \tilde{S}_j(t) \rangle a(t) = \sum_{\sigma=0}^{2^M-1} y(\sigma, t) \sigma_i \sigma_j,$$

:

$$\langle \tilde{S}_1(t) \tilde{S}_2(t) \cdots \tilde{S}_M(t) \rangle a(t) = \sum_{\sigma=0}^{2^M-1} y(\sigma, t) \sigma_1 \sigma_2 \cdots \sigma_M, \quad (2)$$

A dinâmica

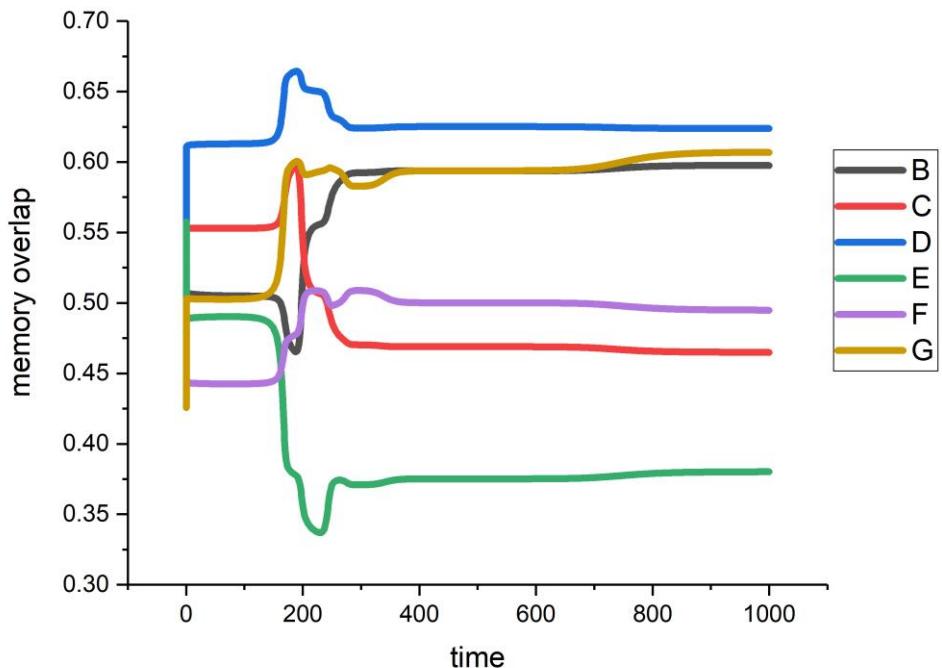
$$y(\sigma, t+1) = [1 - y(\sigma, t)]y(\sigma, t)\lambda(\sigma, t),$$

where

$$\lambda(\sigma, t) = x(\sigma) + \frac{\sum_{\sigma'} z(\sigma, \sigma')y(\sigma', t)}{\sum y(\sigma', t)}.$$

$$x(\sigma) = k_v + (k_m - k_v) \sum_{\mu=1}^P \delta(\sigma, \sigma^\mu),$$

$$z(\sigma, \sigma') = z \delta(\sigma', \sigma^{(i)}),$$



Harvesting information from cells

- + Single cell RNASeq for EMT → data on gene expression.
- + EMT induction by TGFbeta. Measurements at $t=0$, $t=1$ day and $t=8$ days.
- + Results: there are different trajectories.

There are transient, hybrid states

Different cells present different transition rates.

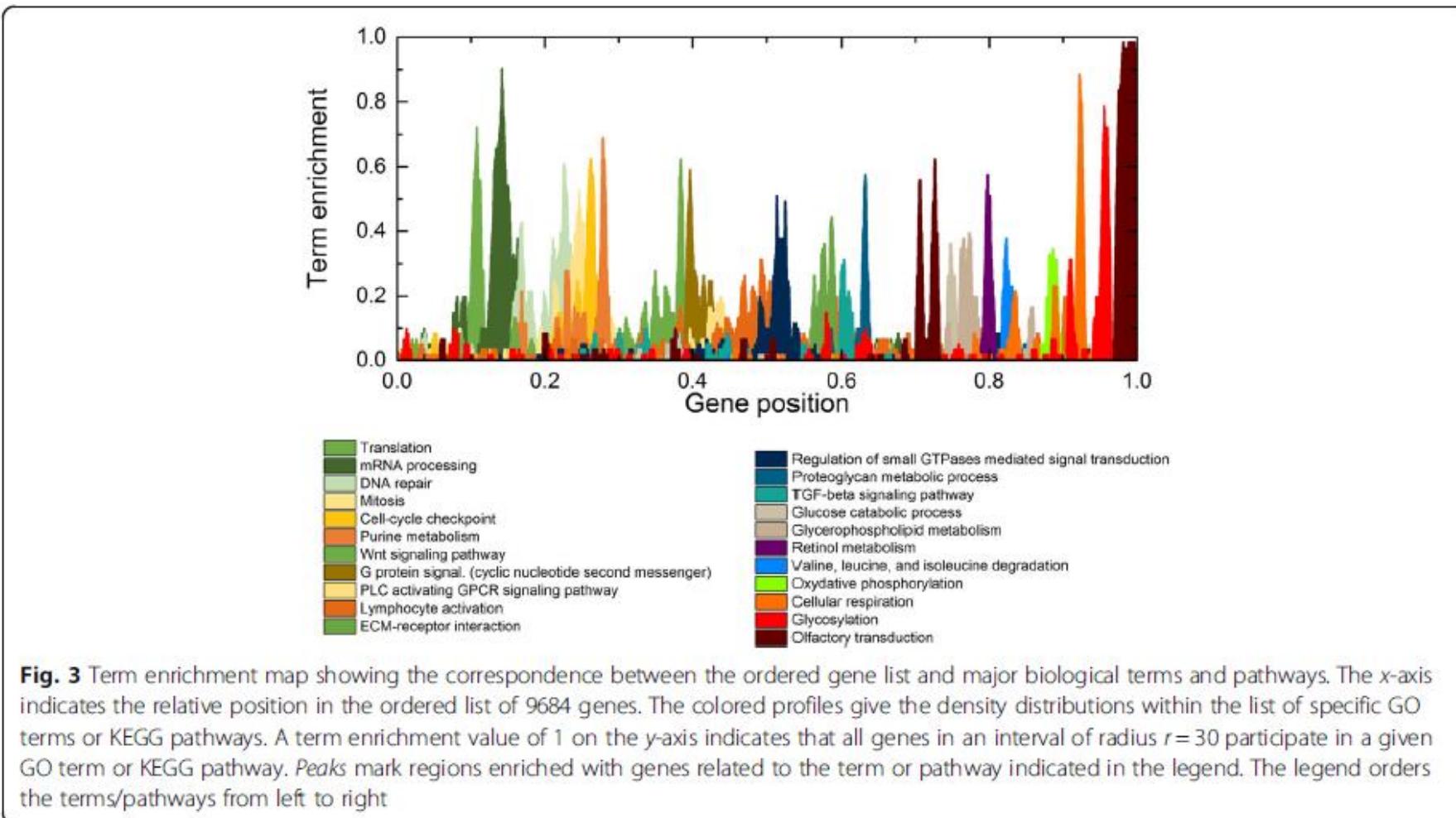
Noise in experimental measurements may represent an issue.

Proposed models do not handle well the dependence with the stimulus application time.

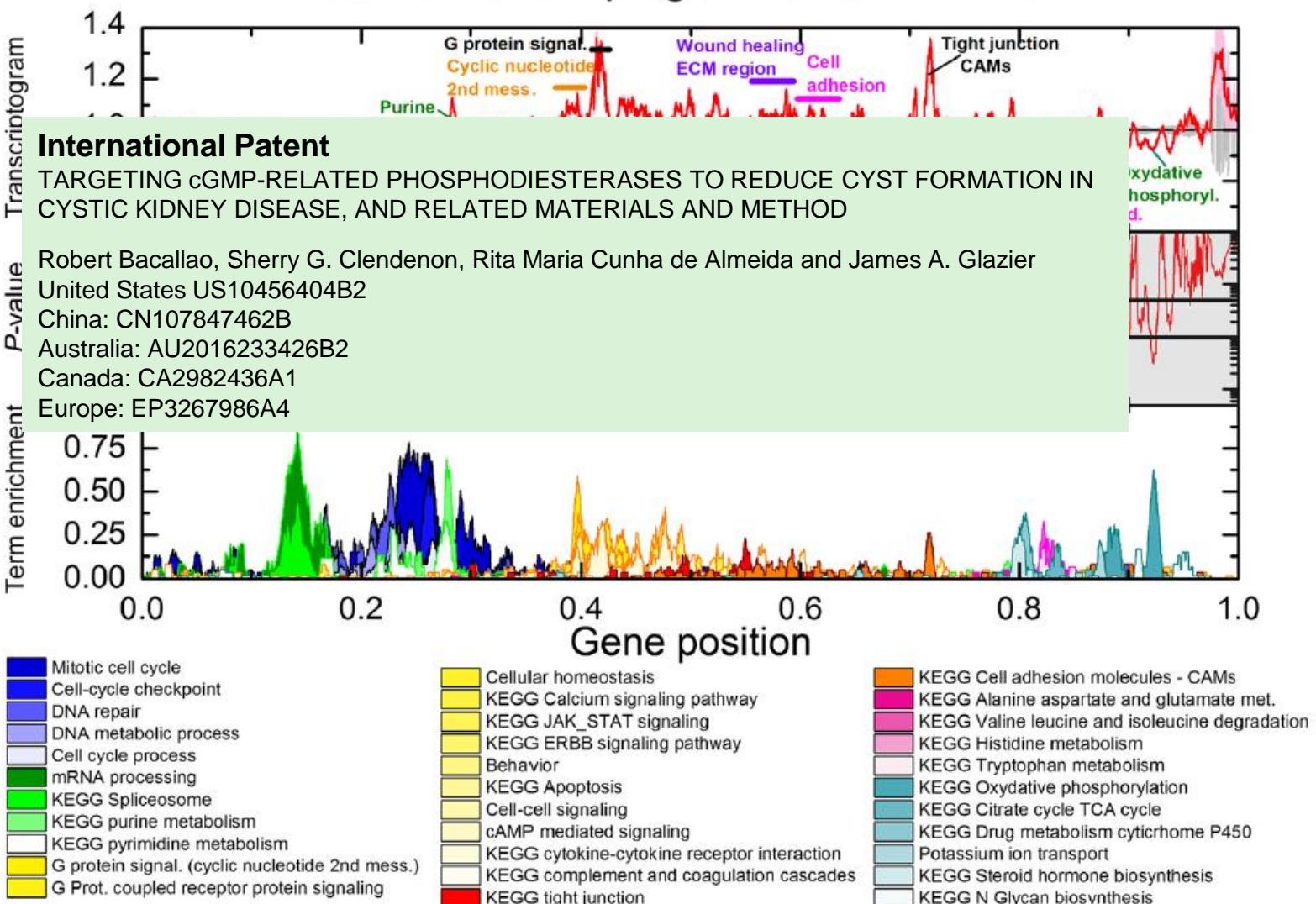
Our proposal: Transcriptograms
Information space dynamics.

Transcriptogramas

Rybarczyk-Filho,..., RMCdeA, Nucleic Acids Research, 2011, Vol. 39 3005–3016
Morais, de Almeida, Dalmolin, Bioinformatics, 2019, 1–2
de Almeida et al. Human Genomics (2016) 10:37



Relative Transcriptogram for C-ADPKD/NK



The project

Metabolic pathways and EMT

- ✓ Model adequation for EMT (work in

Epité

✓ Pas

Mesenchymal

Isolated migrat

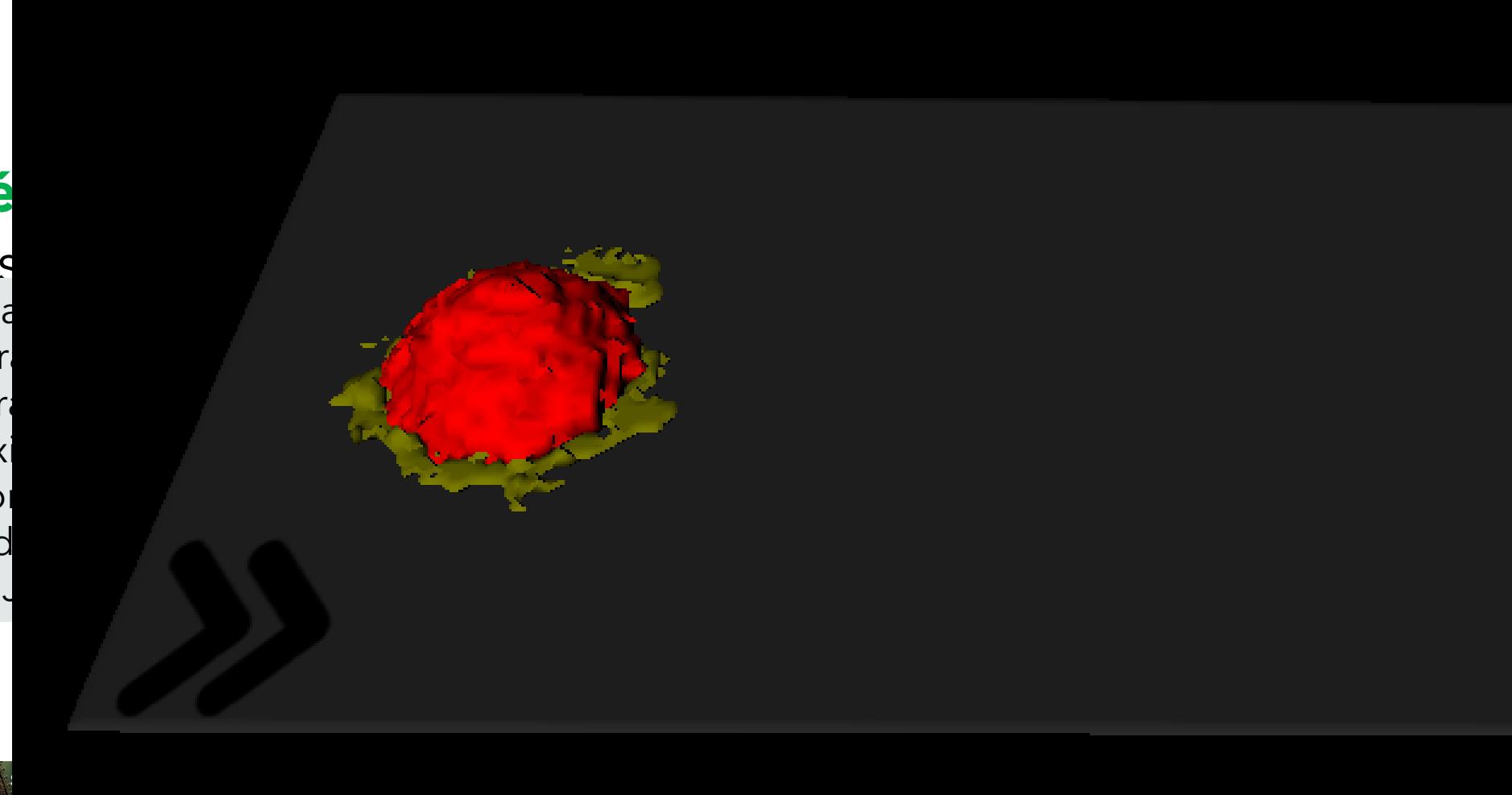
✓ Flat substrat

✓ Chemotaxi

✓ Polarizatio

- Shape and

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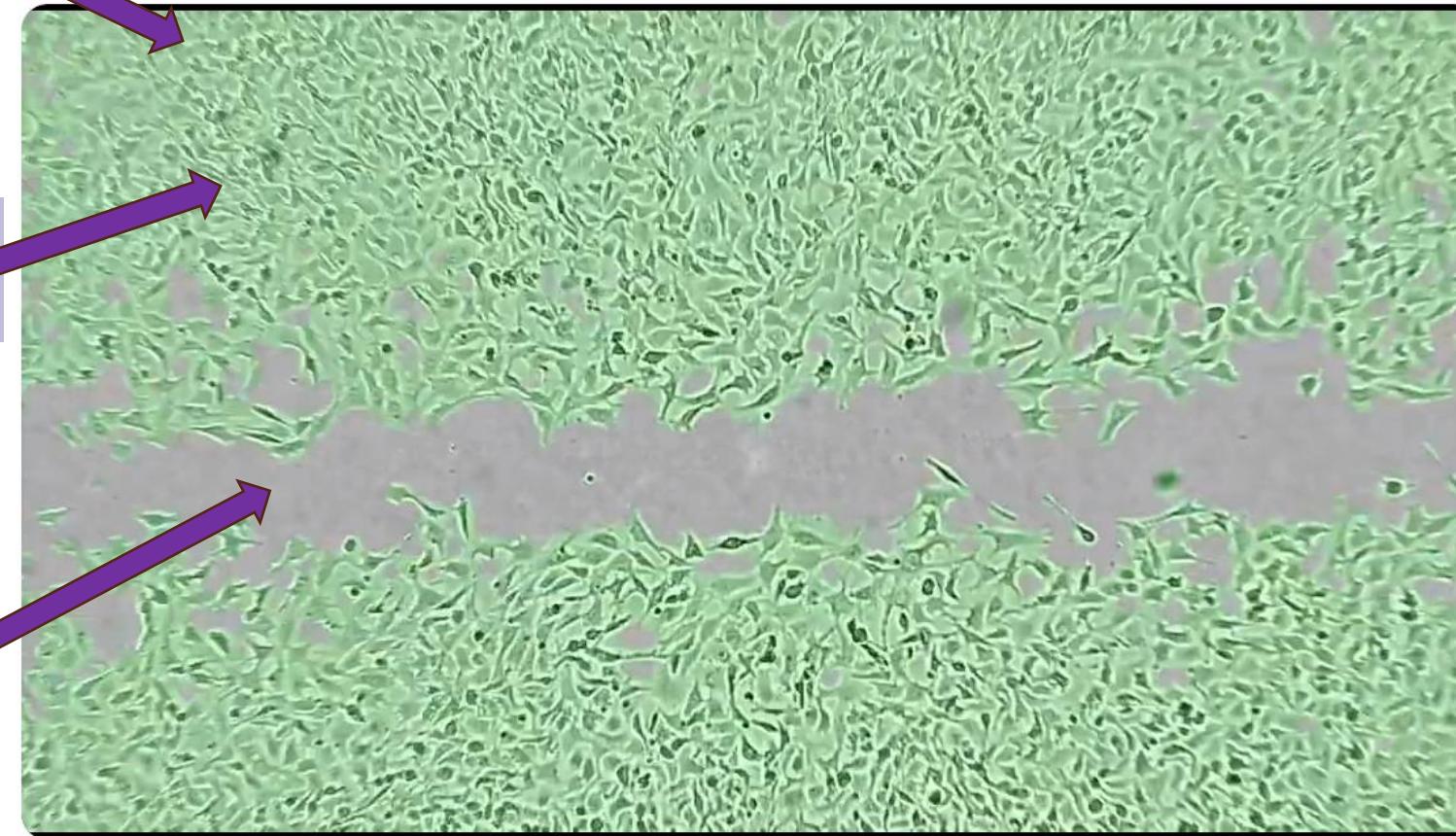
A.CEL

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**Active solids:
epithelium**

**Phenotype
transition**

**Mesenchymal
migration**



Same cellular model

[wound healing assay - Pesquisa Google](#)

Vision and potential e possibilidades

- + Digital twins (precision, personalized medicine)
- + Therapy and drugs
- + Tissue engineering

Thank you!

The computational model: Physics

$$E_{interface} = \sum_{\vec{r}} \sum_{\vec{v}(\vec{r})} J(\sigma(\vec{r}), C(\vec{r}); \sigma(\vec{v}), C(\vec{v})),$$

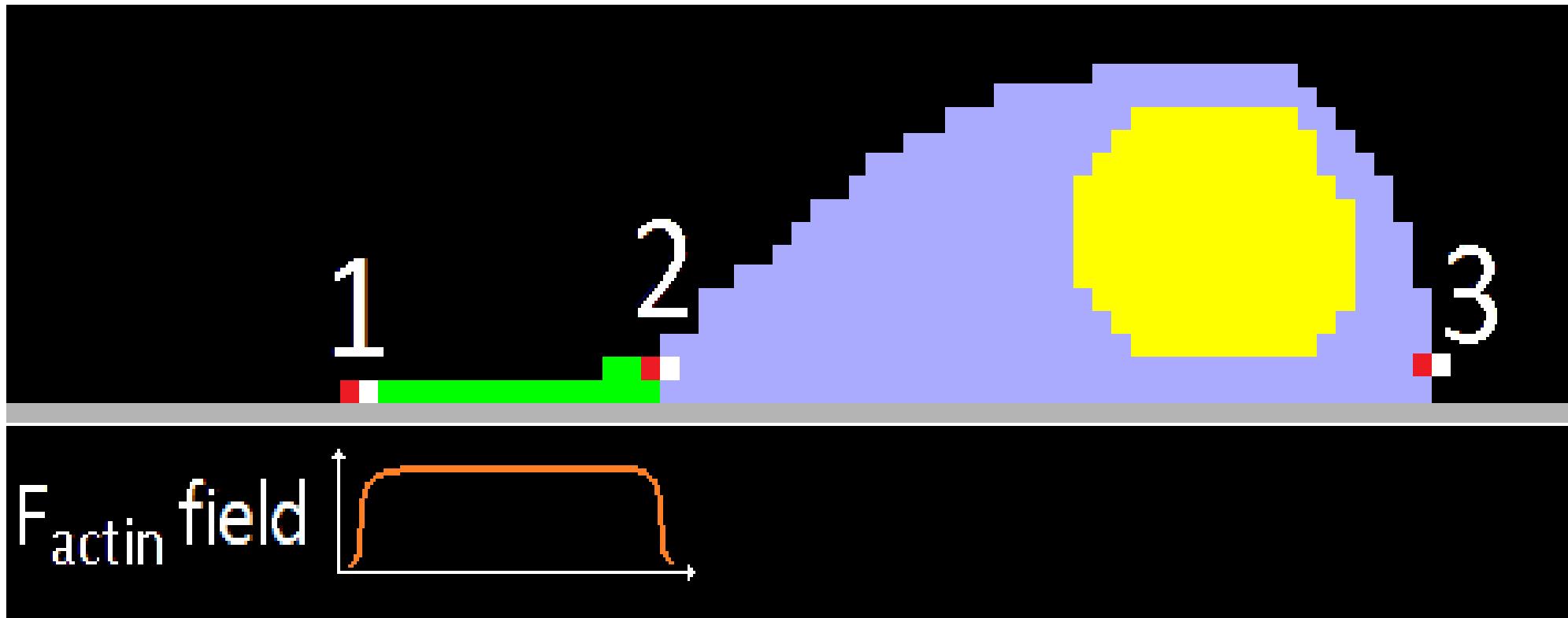
$$E_{target\ volume} = \sum_{C=1}^3 \lambda_C (V_C - V_C^{target})^2,$$

$$E = E_{interface} + E_{target\ volume}$$

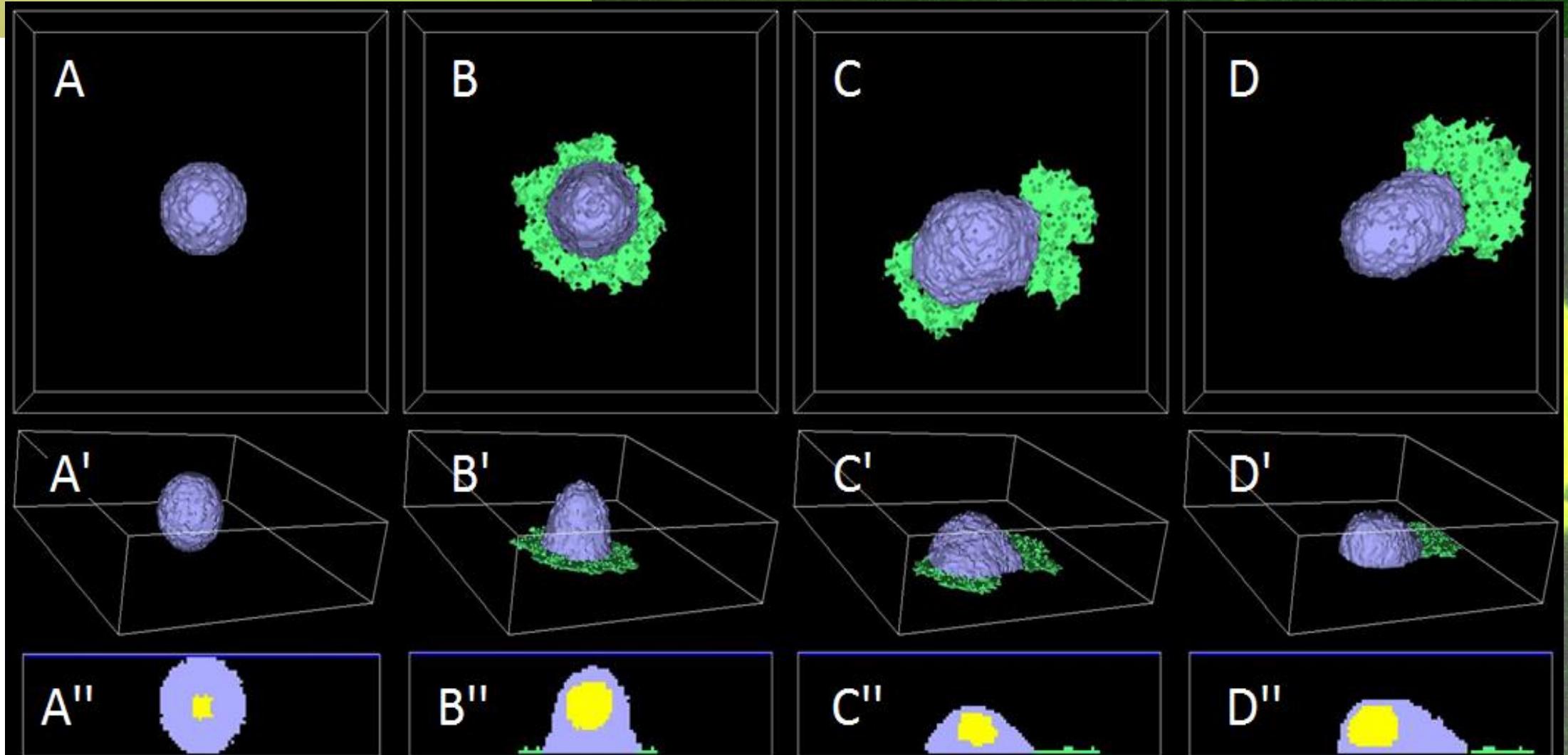
$$\Delta E_{F-actin} = \lambda_{F-actin} [A(\vec{v}) - A(\vec{r})] \delta(C(\vec{r}) - 3) \delta(\sigma(\vec{v}) - \text{medium}),$$

$$\frac{\partial A(\vec{r}, t)}{\partial t} = D_F \nabla^2 A(\vec{r}, t) + k_{source} \delta(C(x, y, z, t) - 3) - k_{decay} A(\vec{r}, t),$$

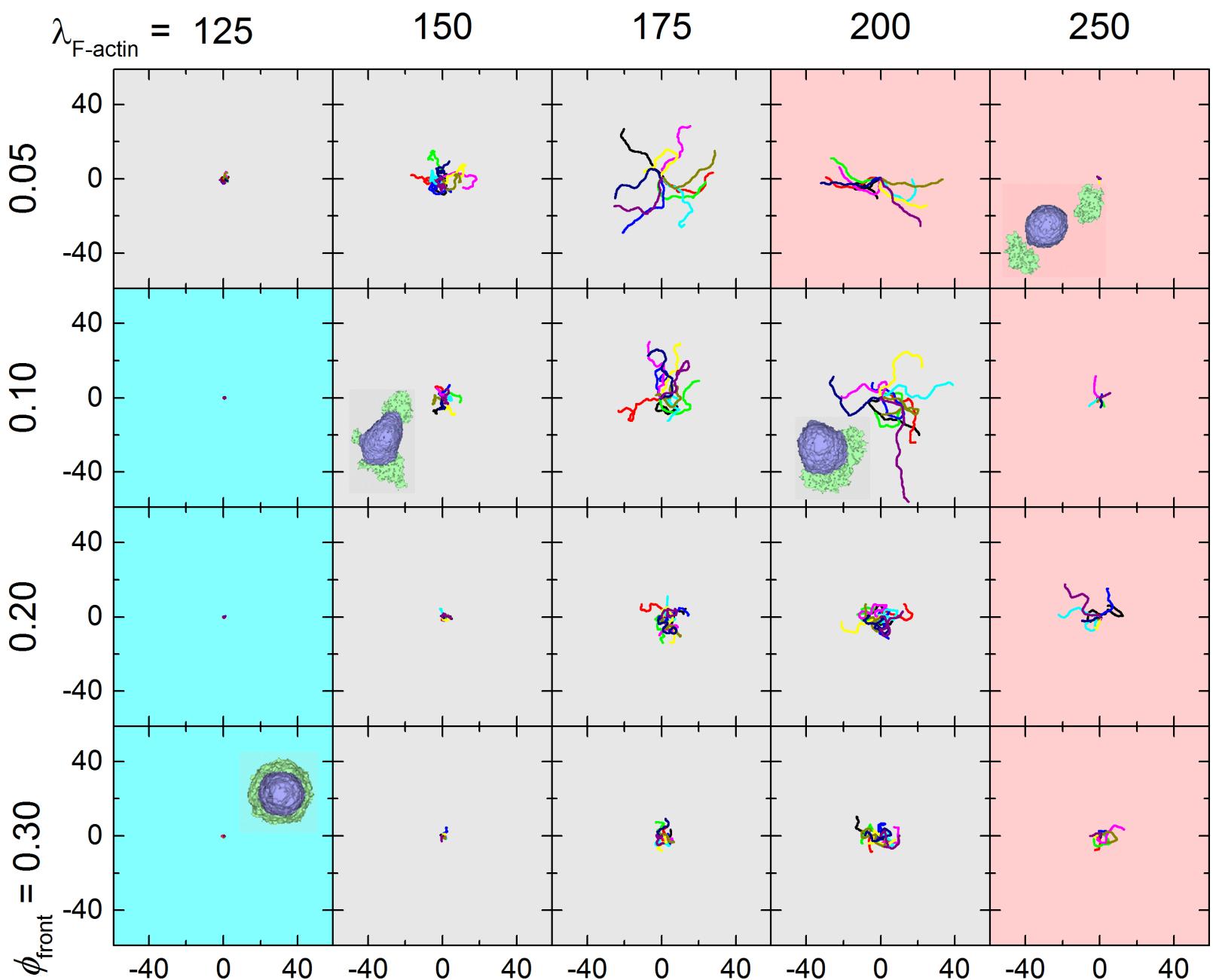
Células mesenquimais: Cellular Potts model

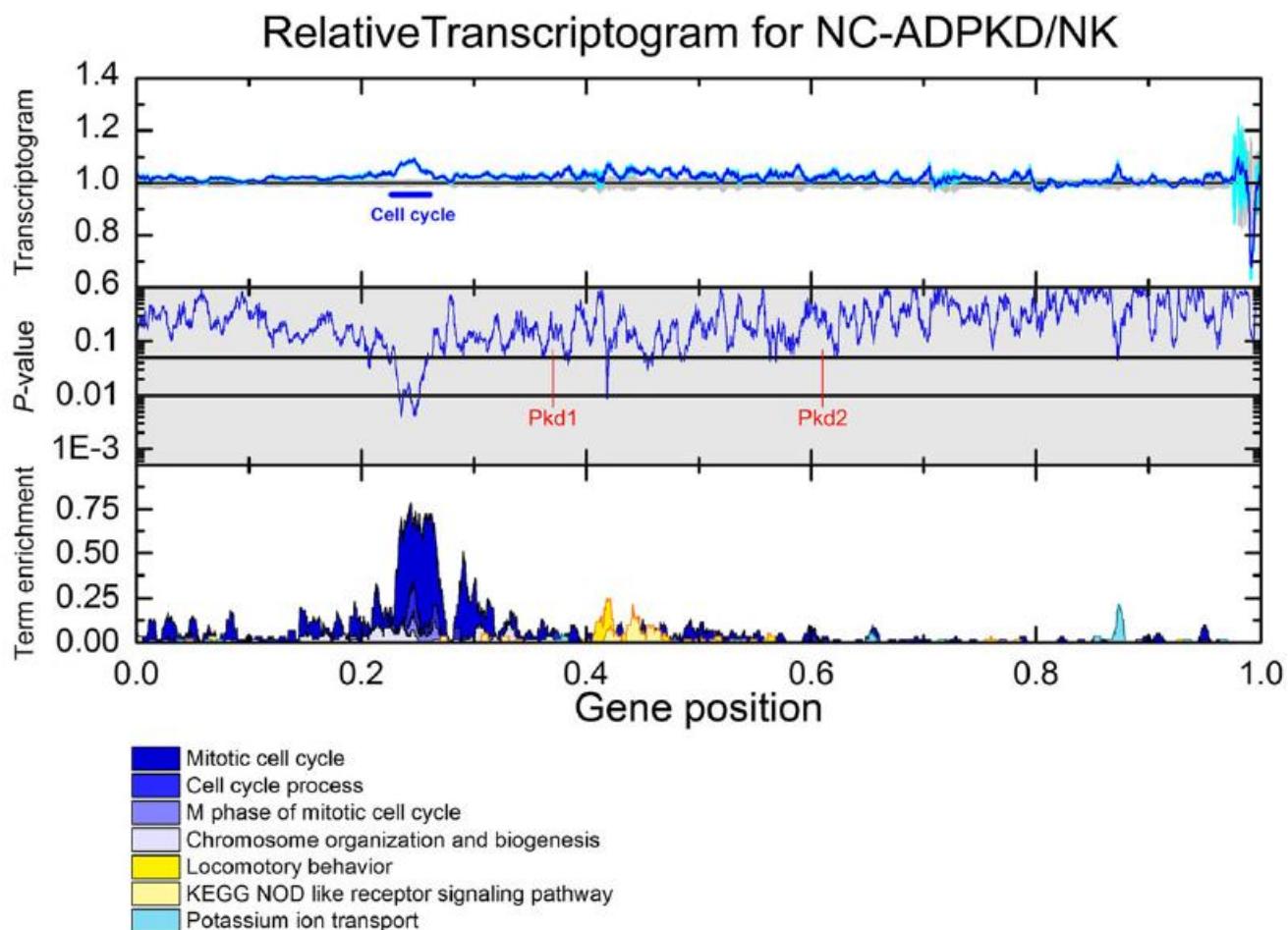


Fortuna, ..., RMCdeA, Biophysical Journal, 118, p 2801, 2020
<https://doi.org/10.1016/j.bpj.2020.04.024>



Simulation Phenotypes





EMT: multiscale, multi-organs, and cellular environment.

- + Cell biochemical alterations;
- + Secretion and reception of molecules;
- + Transport through blood stream.
- + Mechanical interactions (cell-cell adhesions, Cell-ECM adhesions)
- + Quantitative simulations aiming at personal, precision medicine.