

# Learn your entropy from informative data: an axiom ensuring the consistent identification of generalized entropies

Andrea Somazzi<sup>(a)</sup>, Diego Garlaschelli<sup>(a)</sup>

<sup>(a)</sup> *IMT School for Advanced Studies, Lucca*

Generalizations of Shannon entropy, motivated by the study of non-extensive or non-ergodic systems, relax some of SK or SJ axioms and lead to entropy families indexed by certain ‘entropic’ parameters. In general, the selection of these parameters requires pre-knowledge of the system. Here we introduce a simple axiom for any entropy family: namely, that no entropic parameter can be inferred from a completely uninformative (uniform) probability distribution. When applied to the Uffink- Jizba-Korbel and Hanel-Thurner entropies, the axiom selects only Rényi entropy as viable. It also extends consistency with the Maximum Likelihood principle, which can then be generalized to estimate the entropic parameter purely from data, as we confirm numerically. In a generalized maximum entropy framework the axiom implies that the maximized log-likelihood always equals minus Shannon entropy, even if the inferred probability distribution maximizes a generalized entropy and not Shannon’s.